

Logarithms and Exponentials 1

- 1 Watch the video on <u>www.achildsguideto.com</u> → Logs and Exponents → Logarithms Video 1.
- 2 Complete the following exercises.
- 1 Sketch a graph of $y = a^x$ where a>1.



2 Sketch a graph of $y = a^x$ where 0 < a < 1.



3 Fill in the table below to find the values of $y = 2^x$

х	-3	-2	-1	0	1	2	3	4
у	$\frac{1}{8}$				2			



4 Draw a graph of $y = 2^x$.

			1				

5 Using the table below, sketch a graph of $y = 3^x$.

х	-3	-2	-1	0	1	2	3
У							



6 Compare the graphs of $y = 2^x$ and $y = 3^x$. Write a couple of sentences explaining what you notice.



You will find that the y scale needs to be much larger very quickly as the numbers are increasing exponentially. For this reason, we often use graph paper that has a logarithmic scale for y values which would alter the shape of the graph.

1 0 ¹⁰	İ											
10												
10 ⁹												
10 ⁸												
10 ⁷												
10 ⁶												
10 ⁵												
10												
10												
10 ²												
10 ¹												
10 ⁰												→
		1 2	2 3	₿ ∠	4 5	56	5 7	7 8	8 9	91	0	

7 On the graph above, plot $y = 10^x$. What do you notice about the shape of the line?

This is a graph with a logarithmic scale. The shape of the graph allows mathematicians to find patterns in data when it is not initially clear. If the y axis was labelled $\log_{10} x$ instead of y, we could just label the y axis with 0, 1, 2, 3, 4... etc.